

SAT MATH SECTION

Angles



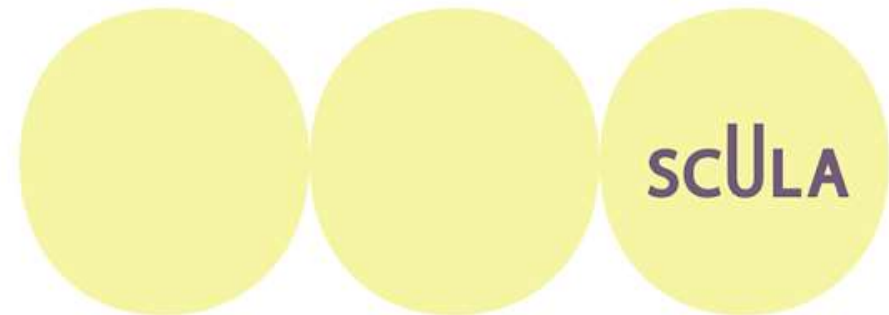
The SAT Geometry has 3 interlinked chapters

1. Angles
2. Triangles
3. Circles



Today we will tackle Angles

These modules will be helpful to understand Triangles and circle over the next sessions



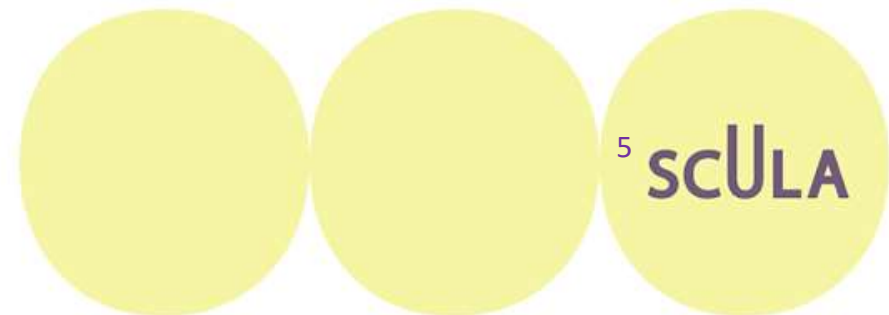
1- Angles

- Exterior Angle Theorem
- Parallel Lines
- Polygons



Both circles and triangles are made of angles .

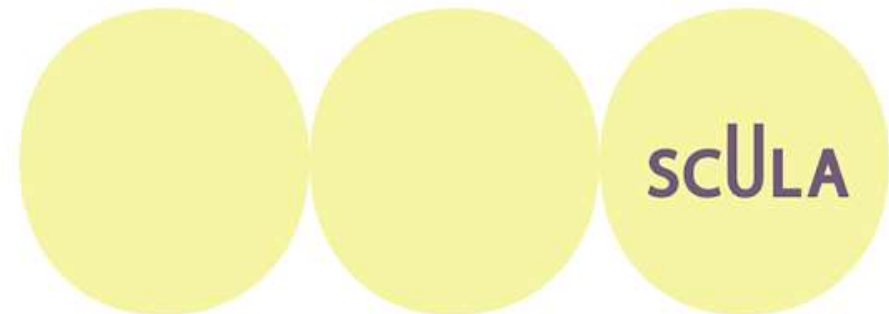
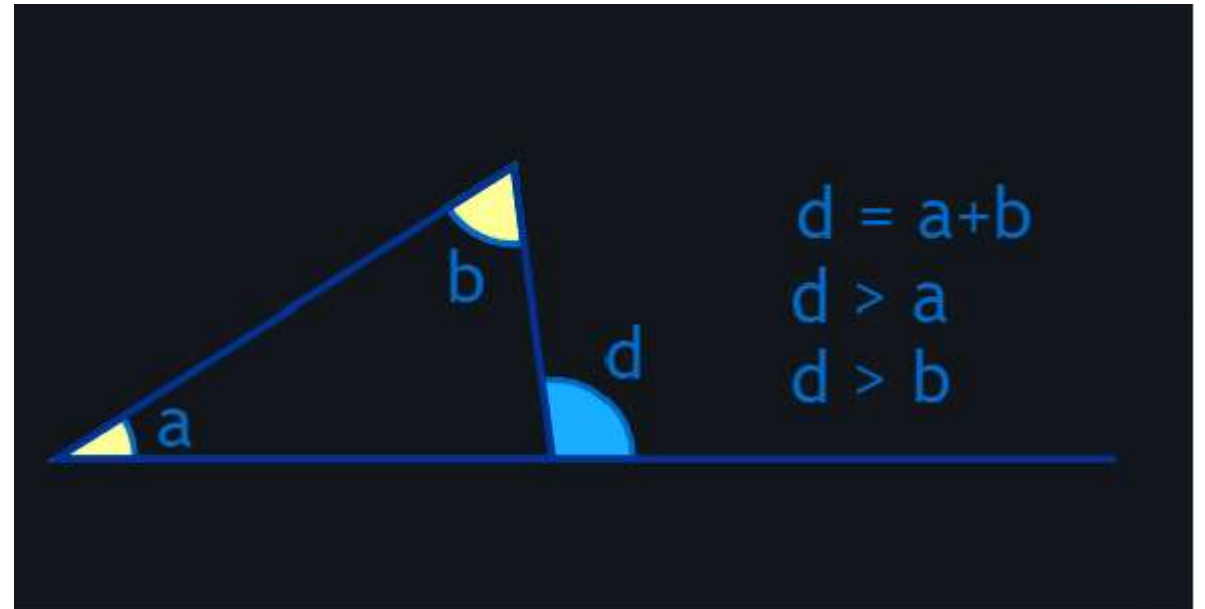
Most questions will require you to find the value of an angle.



What is the measure of the angle d?

Remember these two important rules :

interior angles of a triangle add to 180° , and angles $c+d$ also add to 180°



The interior angles of a triangle add to 180° :

$$a + b + c = 180^\circ$$

Angles c and d make a straight angle, which is 180° :

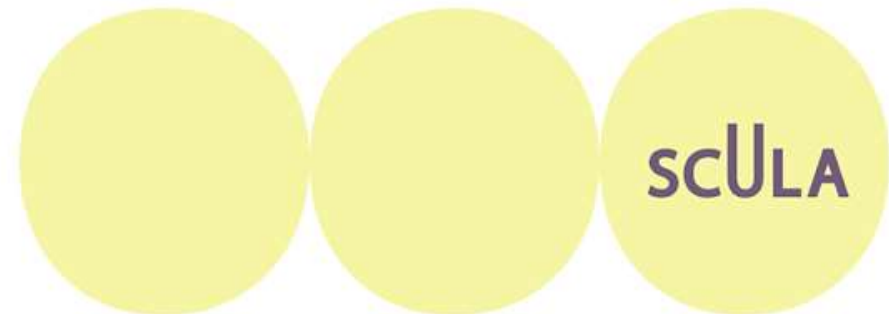
$$d + c = 180^\circ$$

So $d + c$ equals $a + b + c$:

$$d + c = a + b + c$$

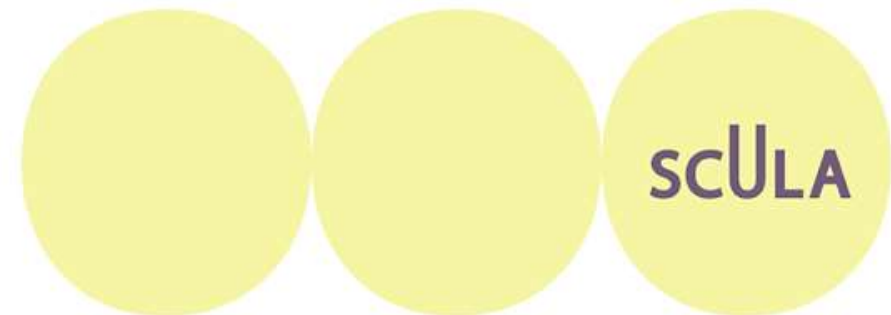
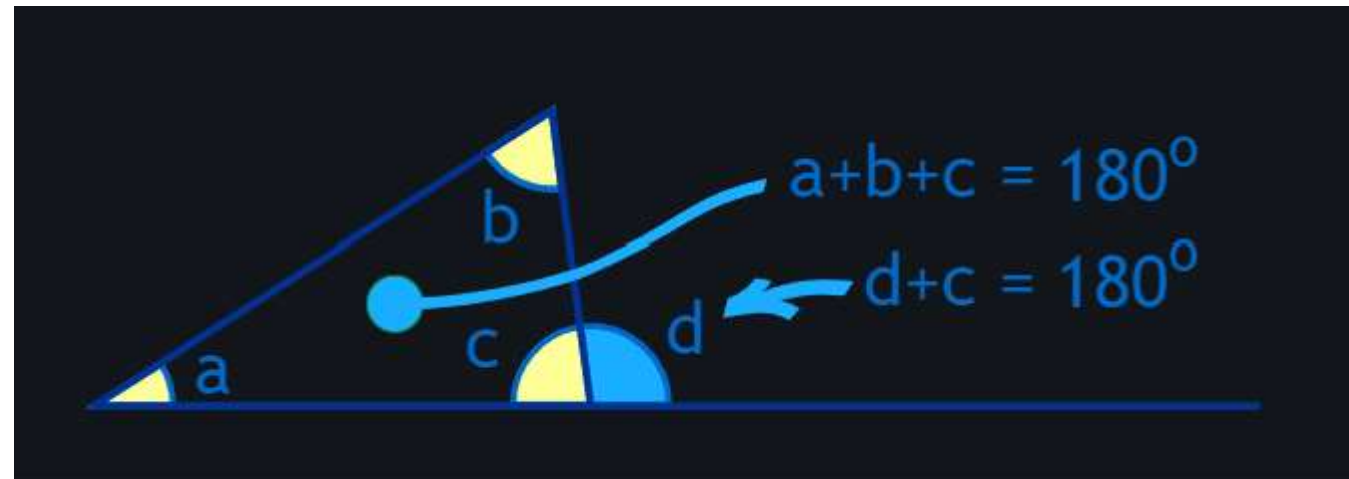
Subtract c from both sides:

$$d = a + b$$



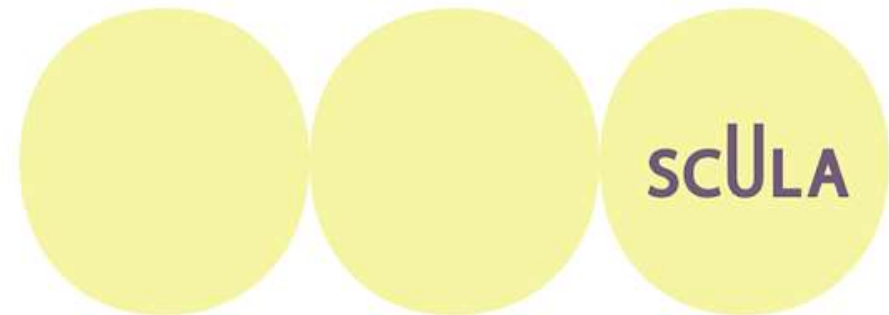
By equating these two relationships between the given angles we can have :

$$a + b = d = 180^\circ - c$$

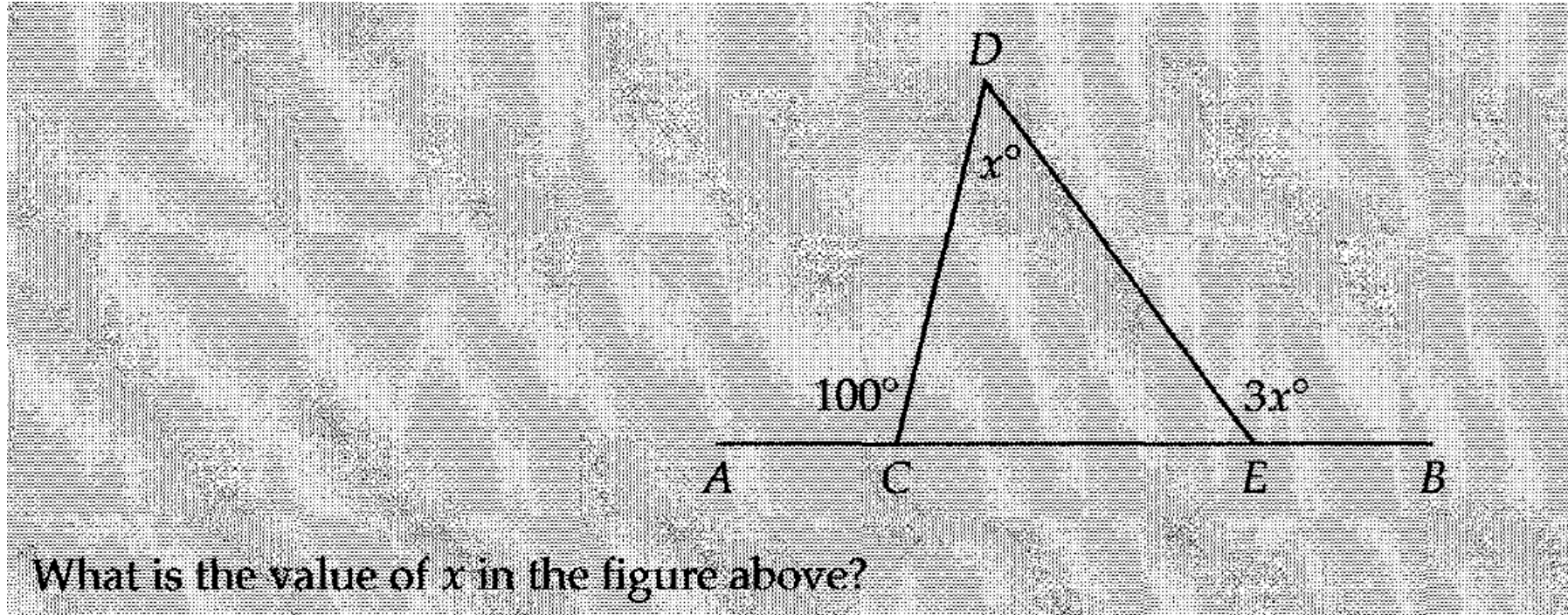


$a + b = d$ is the exterior angle theorem

Now that we have proven this equality, you can use it whenever you come across an exterior angle.



Example :



Apply the exterior angle theorem to solve this question.

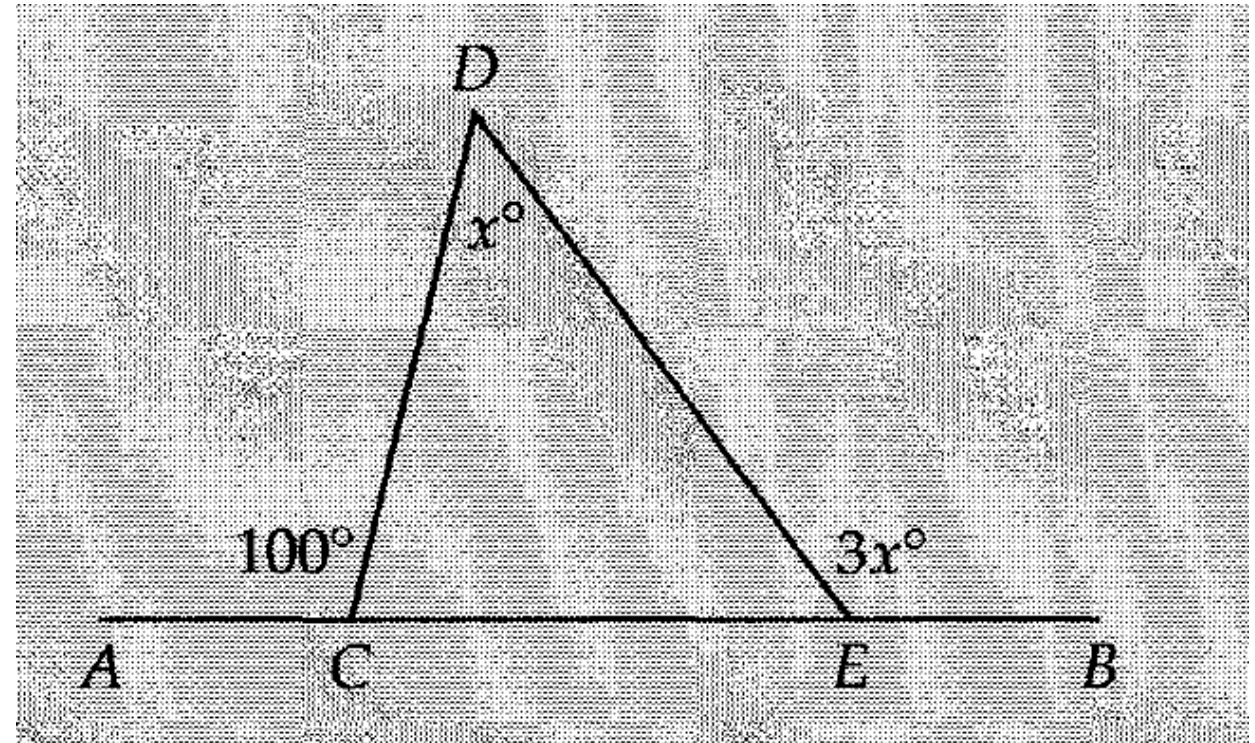
From the figure, we can conclude that $c = 100 - 180$

Applying the theorem on the first exterior angle (exterior angle theorem)
:

$$100 + 80x = 3x$$


$$2x = 80$$

$$x = 40$$



Parallel Lines :

If Any Pair Of ...		Example:
<u>Corresponding Angles</u> are equal		$a = e$
or		
<u>Alternate Interior Angles</u> are equal		$c = f$
or		
<u>Alternate Exterior Angles</u> are equal		$b = g$
or		
<u>Consecutive Interior Angles</u> add up to 180°		$d + f = 180^\circ$
... then the lines are Parallel		



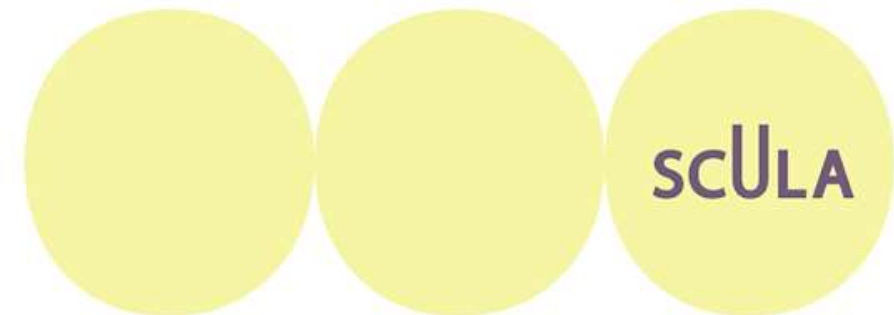
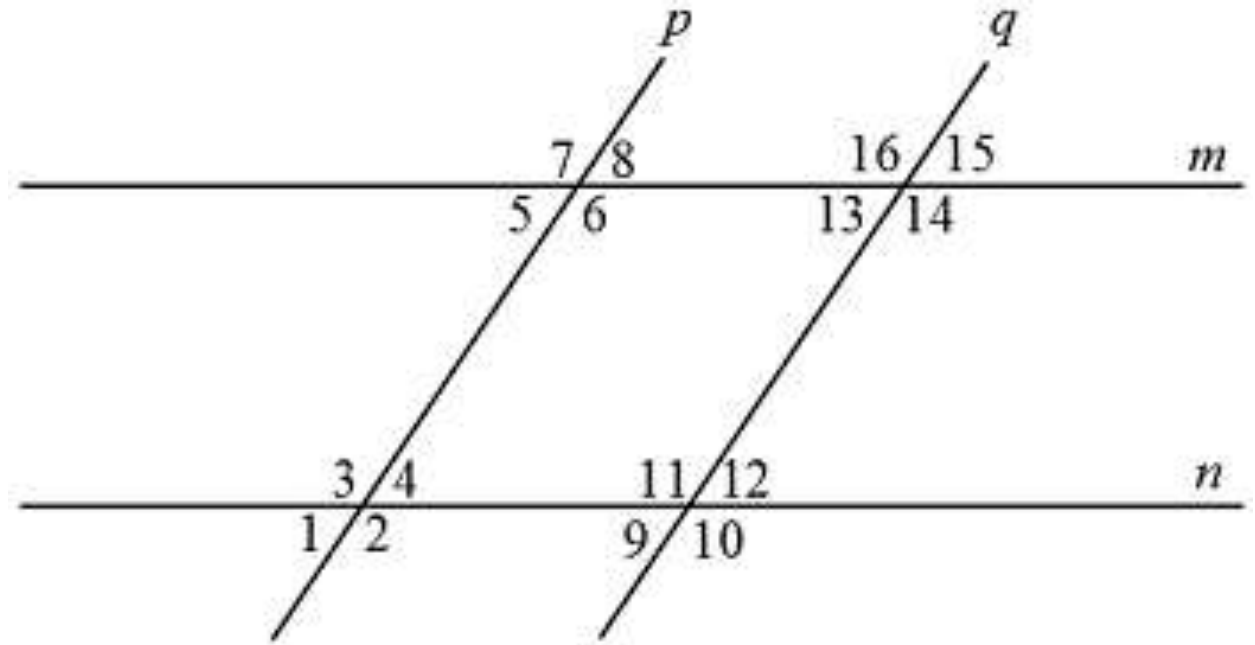
If the lines are parallel and one line intersect both lines, then all the equalities mentioned before apply .

We can conclude for example that :

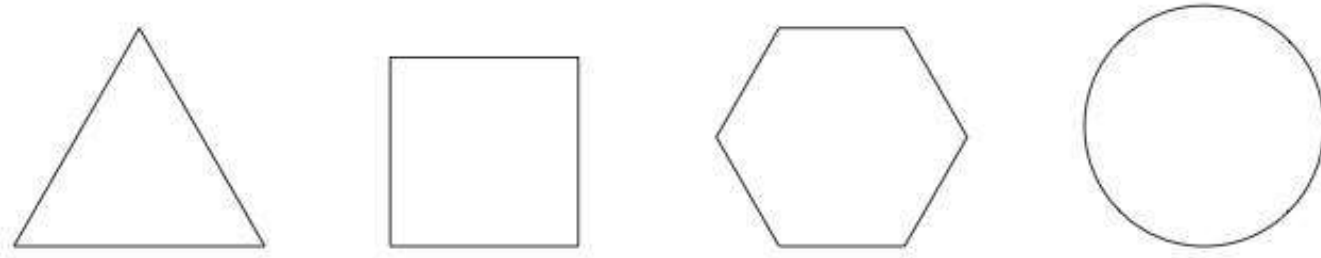
$$12\angle = 9\angle = 4\angle = 1\angle$$

$$5\angle = 1\angle$$

$$16\angle = 11\angle \text{ and } 14\angle = 10\angle$$



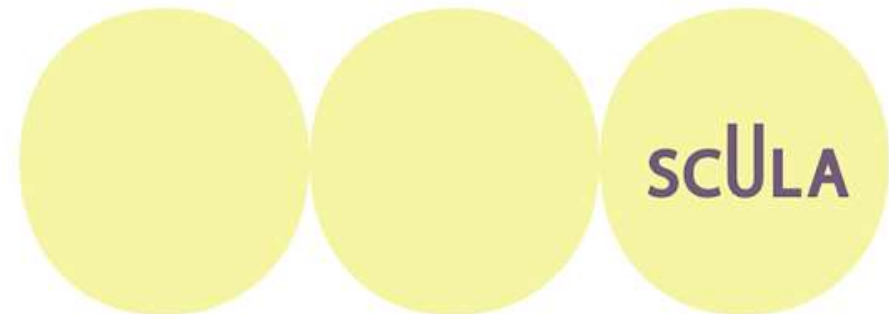
Polygons

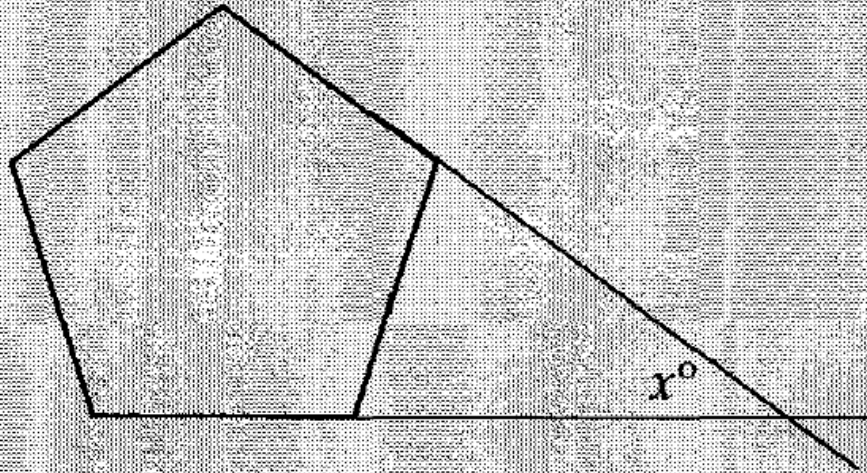


As you can see on the polygons above, each additional side can increase the sum of the interior angles by 180°

For any polygon with n sides, the sum of the interior angles is :

$$S = (n-2)180$$





Two sides of a regular pentagon are extended as shown in the figure above. What is the value of x ?

Remember that a regular pentagon is a pentagon with equal angles and equal sides.

The sum of the interior angle is :

$$540 = (2 - 5)180$$

The measure of one interior angle is :

$$108 = 5 \div 540$$

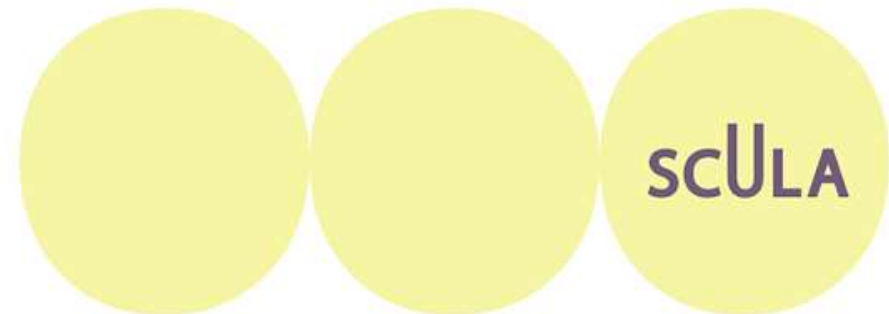
The angles of the triangle formed by intersecting line must be :

$$72 = 108 - 180$$

)The sum of the interior angles of a triangle is (180

The measure of the angle x is:

$$36 = 2 \times 72 - 180$$



THANK YOU!

DO YOU HAVE ANY QUESTIONS?

